

1 37359/JFO/B600

WHAT IS CLAIMED IS:

- 5 1. A method for reducing a precision of an input datum having precision portion and a loss portion, comprising:
- a. comparing the loss portion to a preselected threshold value, f_t ;
- 10 b. determining a selectable bias, α , responsive to the loss portion being in a defined relation to the preselected threshold value, f_t ; and
- c. combining the precision portion with α , creating a reduced precision datum thereby,
- 15 wherein α corresponds to a predetermined characteristic of one of α , the input datum, the reduced precision datum, and a combination thereof.
- 20 2. The method of claim 1, wherein determining the selectable bias further comprises one of:
- a. assigning a first value to α , responsive to the loss portion being substantially equal to f_t ;
- 25 b. assigning a second value to α , responsive to the loss portion being less than f_t ; and
- c. assigning a third value to α , responsive to the loss portion being greater than f_t .
- 30 3. The method of claim 1, further comprising determining the selectable bias responsive to a predetermined characteristic
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1 37359/JFO/B600

of a plurality of input data relative to a corresponding
plurality of reduced precision data.

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4. The method of claim 1, further comprising determining the
selectable bias responsive to a predetermined characteristic
attributable to reducing the precision of the input datum.

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5. The method of claim 1, further comprising determining the
selectable bias responsive to the predetermined
characteristic of the selectable bias, the predetermined
characteristic being the mean value of a plurality of
selectable bias values.

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6. The method of claim 2, further comprising determining the
selectable bias responsive to a predetermined characteristic
of a plurality of input data relative to a corresponding
plurality of reduced precision data, and the predetermined
characteristic being attributable to reducing the precision.

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7. The method of claim 6, wherein the predetermined
characteristic is a predetermined mean error value.

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8. The method of claim 2, further comprising determining the
selectable bias responsive to a predetermined characteristic

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1 37359/JFO/B600

of one of input data, a corresponding reduced precision
data, and a combination thereof.

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9. The method of claim 8, wherein the predetermined
characteristic comprises a predetermined statistical value.

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10. The method of claim 4, wherein the predetermined
characteristic comprises a predetermined mean error value
of the plurality of reduced precision data relative to a
corresponding plurality of input data.

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11. The method of claim 9, wherein the predetermined statistical
value comprises the mean value of the reduced precision data
relative to a corresponding plurality of finite-precision
fixed point input data.

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12. The method of claim 2, further comprising assigning a fourth
value to α , responsive to a being substantially equal to f_t ,
the fourth value being in a predefined relationship with the
first value.

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13. The method of claim 12, further comprising determining the
selectable bias responsive to a predetermined characteristic
of input data relative to corresponding reduced precision

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1 37359/JFO/B600

data, and the predetermined characteristic being a
preselected mean error value associated therewith.

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14. The method of claim 12, wherein:

a. the f_t is approximately equal to 0.5_{10} ;

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b. the first value is 1 when the value of the loss
portion substantially equals about 0.5_{10} , the input
datum is a negative-valued datum, with the first value
being added to the precision portion;

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c. the second value is zero when value of the
loss portion is less than about 0.5_{10} ;

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d. the third value is 1 when the value of the loss
portion is greater than about 0.5_{10} , with the third
value being added to the precision portion;

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e. the fourth value is 0 when the loss portion
substantially equals about 0.5_{10} , and the input datum is
a positive-valued datum; and

f. the preselected mean error value relative to the input
datum and the reduced precision datum is minimized.

30 15. The method of claim 11, wherein:

a. f_t is substantially equal to 0.5_{10} ;

b. the first value is a current first value being
selected to be one of '1' and '0' when the value of

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1 37359/JFO/B600

the loss portion substantially equals about 0.5_{10} , in
a predefined relationship to a previous first value;
5 c. the second value is zero when the loss portion is less
than about 0.5_{10} ; and
d. the third value is 1 when the loss portion is greater
10 than about 0.5_{10} , with the third value is added to the
value of the precision portion.

16. The method of claim 14, wherein the predefined relationship
15 is an alternating relationship.

17. The method of claim 16, wherein the alternating relationship
is a toggle relationship with the current first value being
20 zero if the previous first value was 1, and the current
first value being 1 if the previous first value was zero,
and wherein the preselected mean error value is minimized
responsive to the alternating relationship.

18. The method of claim 15, wherein the alternating relationship
includes a selectable number of 1's being interleaved with
30 a selectable number of zeros, the mean value of the reduced
precision data being responsive to the alternating
relationship.

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1 37359/JFO/B600

19. The method of claim 2, wherein each of the input datum and
the reduced precision datum are represented by two's
5 complement fixed point values.

20. The method of claim 16, wherein the alternating relationship
10 includes a selected pseudorandom sequence of data bits.

21. A method for rounding a first datum, X , having precision of
 a digits, to a second datum, X' , having precision of b digits,
15 wherein $a > b$, first b digits of X being a precision portion, and
remaining $a-b$ digits of X being a loss portion, the method
comprising:

a. evaluating the loss portion relative to a preselected
20 rounding threshold value;

b. if the loss portion is substantially equal to the
preselected threshold, then defining X' according to
the equation:

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$$X' = X + 2^{-(b+1)}\alpha,$$

where α is a selectable bias represented by a rounding
digit;

30 c. if the loss portion is not substantially equal to the
preselected threshold, then defining X' according to
the equation:

$$X' = X + 2^{-(b+1)}; \text{ and}$$

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d. eliminating the loss portion of X , producing X thereby.

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22. The method of claim 21, wherein selectable bias α is representative of a predetermined characteristic of one of X , X , α , and a combination thereof.

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23. The method of claim 22, wherein the preselected threshold is substantially equivalent to 0.5_{10} .

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24. The method of claim 23, wherein the predetermined characteristic comprises a preselected mean error value of X relative to X .

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25. The method of claim 24, wherein the preselected mean error value, $E(e)$, is substantially defined by the equation:

$$E(e) = 2^{-a}(E(\alpha) - \frac{1}{2}),$$

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where $E(\alpha)$ is a mean value of selectable bias α .

26. The method of claim 25 wherein the mean value of the selectable bias is substantially within the range of

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$$0.0 \leq E(\alpha) < 1.0$$

27. The method of claim 26, wherein the mean value of the selectable bias, $E(\alpha)$, is approximately equal to

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1 37359/JFO/B600

preselected mean error value, $E(e)$, and $E(\alpha)$ is approximately zero.

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28. The method of claim 27, wherein the predetermined characteristic further comprises a preselected error variance value, σ_e^2 , substantially defined by the equation:

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$$\sigma_e^2 = \frac{2^{-2b} + 2^{-(2a-1)}}{12}$$

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29. The method of claim 28, wherein the rounding digit is selected from a alternating sequence of digits in the pair of digits $\langle 0, 1 \rangle$.

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30 The method of claim 28, wherein the rounding digit is selected from a pseudorandom sequence of binary digits.

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31. A method for rounding a first two's complement fixed point datum, X , having an integer part of n bits, a fractional part of a bits the integer part, and sign bit, s_i , to a second two's complement fixed point datum, X' , having a fractional part of b bits following the radix point, where a and b are representative of the respective precisions of X and X' , and where $a > b$, comprising:

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1 37359/JFO/B600

a. evaluating the fractional part of X and defining y as the most significant bit (MSB) of the a bits;

5 b. if the first bit following the radix point of X is equal to a 1 bit trailed by $(a-1)$ zero bits, then defining \hat{X} according to the equation:

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$$\hat{X} = n + s_1$$

and

c. otherwise, defining \hat{X} according to the equation:

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$$\hat{X} = n + y$$

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32. The method of claim 31, wherein the occurrence of positive numbers and negative numbers in a plurality of the datum, X , is substantially equiprobable.

33. A method for rounding signal values, comprising:

25 a. detecting a predetermined state value wherein rounding is desired; and

b. rounding the state value according to one of

i. an alternating round-up/round-down method and

30 ii. a sign addition round-up/round-down method.

34. An arithmetic device, comprising a bias generator producing a selectable bias α , responsive to a predetermined signal characteristic, the device receiving an input signal and

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1 37359/JFO/B600

coupling the selectable bias α thereto.

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35. The arithmetic device of claim 34, further comprising a combiner coupled to the bias generator, the combiner receiving and combining the input signal and the selectable bias α , and producing an output signal.

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36. The arithmetic device of claim 34 further comprising wherein the bias generator further comprises a comparator for comparing the input signal to a preselected threshold value, the comparator urging the bias generator to produce the selectable bias α responsive to the preselected threshold value.

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